RELIABILITY ANALYSIS OF INTERPOLATION METHODS IN TRAVEL TIME MAPS – THE CASE OF WARSAW

STATISTIČNA ANALIZA ZANESLJIVOSTI INTERPOLACIJSKIH METOD NA KARTI ČASOVNE DOSTOPNOSTI – PRIMER VARŠAVE

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ABSTRACT

Describing the accessibility, by public transport, of a given place is of particular importance today. The speed and multiplicity of urban public transport have made many places far more accessible than they were at the beginning of the 20th century. Descriptions of the accessibility of a given place, expressed in terms of travel time, have been carried out since the 19th century, when the first map for journeys to London by public transport was published. Since then, many "accessibility maps" have been produced and the theoretical principles for their creation drawn up. However, the influence that particular methods for interpolating travel times have on the accuracy and appearance of such maps has not been analysed.

The purpose of this article is an analysis of interpolation methods, using a tool such as GIS, for estimating the accessibility of any location. The research was conducted by the Military University of Technology in Warsaw (MUT), drawing up an isochrone map that showed travel times by public transport to the MUT campus. According to the results, the lowest mean absolute percentage error (MAPE) and mean absolute error (MAE) were shown applying the IDW method, in which small isochronic islands did not appear. The highest estimation errors occurred with the nearest neighbour method, and the least beneficial arrangement of isochronic islands appeared using the spline method.

KEY WORDS

isochrone, interpolation, accessibility, travel time map, interpolation errors

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Določanje dostopnosti območja s sredstvi javnega prevoza je zelo pomembno. Zaradi velikosti in hitrosti sredstev mestnega prevoza so marsikateri kraji bolj dostopni kot na začetku 20. stoletja. Strokovnjaki so določali dostopnost območja, ki jo izraža čas prispetja na cilj, že v 19. stoletju, ko so izdali prvo karto javnega prevoza v Londonu. Od takrat je nastalo veliko kart dostopnosti. Poleg tega imamo na voljo teoretična pravila oblikovanja kart. Kljub temu nismo še analizirali vpliva metode interpolacije časa vožnje na točnost in obliko kart dostopnosti. Cilj tega prispevka je analiza metod interpolacije, ki so na voljo v programih tipa GIS, za aproksimacijo dostopnosti na poljubnem kraju. Raziskava je bila opravljena na višji šoli Wojskowa Akademia Techniczna (Vojaška tehniška akademija). Njen namen je bil oblikovanje izohron, ki prikazujejo čas vožnje z javnim prevoznimi sredstvi na akademijo. Izidi so dokazali, da je najmanjša napaka interpolacije značilna za metodo IDW, čeprav ta metoda ne registrira majhnih izohronih otokov. Največ napak interpolacije je bilo v metodi »najbližjega soseda«, najmanj koristna lega izohronih otokov pa je bila v metodi »spline«.

KLJUČNE BESEDE

izohrona, interpolacija, dostopnost, karta časovne dostopnosti

1 BACKGROUND. FROM GALTON'S MAP TO A GLOBAL MAP OF ACCESSIBILITY

Accessibility describes the length of travel time to a chosen location by different modes of transport (land, water and air). This time is most often visualised with the aid of an isarithmic method, by way of an isochrone¹ or an isodapane². The author of the first study to describe the accessibility, expressed in time, of a given location was Francis Galton. In 1881 he drew up an Isochronic Passage Chart for Travellers, a map that displayed the travel time to London, from anywhere in the world, via generally available modes of public transport (Galton, 1881). He marked those locations that were accessible in an equal time with isolines and named them isochrones. In the following decades, location accessibility was the object of research by both cartographers and geographers, and in latter years, urban planners and economists. The most valuable source of information concerning methods for describing accessibility time and its cartographic representation are the works of geographers and cartographers from the beginning of the 20th century, including Hassinger (1903), Schjerning (1903), Riedl (1911), Eckert (1925), Rewienska (1929), Kubijowicz (1923), Boczar (1933) as well as the recent work of mainly British scientists, such as Carden (2005), Nelson (2008), Lightfoot and Kelly (2006), as well as Lightfoot and Steinberg (2006). The time accessibility was also key element of industrial location model, introduced in the first decade of 20th century by Weber (Weber, 1929).

The accessibility maps drawn up differ in scale, mapped area, and methods for calculating travel time, as well as the mode of transport considered. The authors of *accessibility maps* (also known as *time contour maps* or *travel-time maps*) draw attention to the fact that isochrones vary depending on whether private transport, in addition to public transport, is considered in the calculations (Witt, 1970; Pietrusiewicz, 1996; Schurmann, 1999; Lightfoot and Kelly 2006; Lightfoot and Steinberg, 2006; Street, 2006). Isochrones for private transport generally have an elongated shape that follows the course of roads. In contrast, isochrones for public transport, which is limited by routes, stops and timetables, normally have a circular shape, thereby creating so called *isochronic islands*, the centres of which correspond to the location of stops or stations. When the accessibility of an area is analysed, and only public transport is considered, one result is the appearance on the map of 'inaccessible' areas, that is, areas from which it is impossible to reach the chosen destination. Analysis of all modes of transport, including private transport, enables the creation of one continuous surface uninterrupted by isochronic islands.

One example of this type of study is the *Global Accessibility Map*, made by the Joint Research Centre in Ispra for the World Bank (Nelson, 2008; Williams, 2009; World Bank Report, 2009). The map shows that barely 10% of the Earth's land area is more than 48 hours away from towns with a population of 50,000 or more.

The approach to calculating location accessibility had changed markedly by the end of the 1990s. A multitude of computer applications have facilitated and made faster the tedious task of calculating travel times, making it possible to apply different interpolation methods and *cost-distance* algorithms, and also increasing the area to which the method can be applied. The methodological basics for creating accessibility maps by using geographic information systems

- ¹ The curve for which the transportation means starting at one or different points finish at the same time after being released.
- ² The curve for which the travel or transportation starting at one or different points have de same costs of transport.

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are described in many research papers (Juliao, 1997; Koening, 1980; Schurmannn, 1999; Street, 2006; Nelson, 2008; Müller and Glander 2010).

Location accessibility is the basis for drawing up area development strategies (EPSON, 2009; Feltynowski, 2009; Bogataj and Drobne, 2010; Zavodnik Lamovsek and Drobne, 2011), space management plans and studies (Bogataj and Drobne, 2005, 2010; Drobne, Lisec and Bogataj, 2008; Zegda, 2009), regionalisation, development of particular transport networks (Kaczmarek, 1978; Schurmann, 1999; Lighfoot and Kelly, 2006), as well as tourism and recreation development (Novosad, 1980). It is a significant factor involving the development of suburbanisation (Nelson, 2008), development of the property market (Carden, 2005) and also access to education (Guzik, 2003). In the last few years, we have seen the advent of web-based tools for presenting and analysing travel times. The most interesting applications are *Travel Time Tube Map* (Carden, 2005) and MySociety *Travel-time maps* (Lightfoot and Kelly, 2006; Lightfoot and Steinberg, 2006). The visualisation of travel times, using open data and web-based tools, creates new opportunities for individuals, and public and private organisations. It makes it easy to analyse commuting times without specialist software or expert skills (Müller and Glander, 2010).

Despite a great deal of work in the research field, the different interpolation methods used to define the accessibility of each point of a studied area in relation to a destination point have not been evaluated and, most often, not even mentioned. It is therefore unknown by what method location accessibility is described, what is the error in describing this accessibility and also how the choice of interpolation algorithm influences the accuracy of the results. Endeavouring to fill this gap in the studies undertaken to date, the authors performed an evaluation of the surface interpolation methods used for preparing time-contour maps.

2 OBJECT AND METHOD OF RESEARCH

2.1 Calculation of travel time

Determining location accessibility by means of the surface interpolation method requires:

- (1) A decision whether to prepare a "mono" (single destination point) or "polycentric" (multiple destination point) map.
- (2) Choice of transport mode and measurement points (quantity and distribution) and method for calculating travel time:
 - a. according to theoretical time, which is derived from permissible speeds and distances ("theoretical" isochrones) or the time listed in timetables ("actual" isochrones);
 - b. calculated time from the starting point to the exterior ("centrifugal" isochrones) or calculated from the boundaries of the studied area towards the destination point ("centripetal" isochrones).
- (3) Determination of travel time between stops (measured points).
- (4) Selection of interpolation method and performance of calculations.
- (5) Accuracy assessment of results.
- (6) Travel time visualisation.

The key elements of this process are the choice of methods for both travel time calculation and interpolation.

There is no agreement in the literature concerning the optimum method of travel time calculation. Different authors, depending on the size of the analysed area, and the scale of the study, choose varying methods for calculating travel time, taking into account shortest travel time, average time, maximal or time repeated most frequently in timetables and also time spent waiting and making connections (for bus or train). The time taken to reach a bus stop or station is most often accounted for only in large and medium scale studies. The accessibility of a specified place is a function of the location of the starting and ending points of a journey, the length of travel time, accessibility of transport, and cost preference. In order to calculate the total length of travel time (door-to-door), it is necessary to include the time taken to reach a bus stop or station, the time spent waiting for public transport to arrive and also the travel time itself, which may be expressed by the formula (Davis, 1986; Schnabel and Lohse, 1997).

$$T = t_d + \sum_c t_c + \sum_p t_p \tag{1}$$

where:

- T total length of travel time,
- t_d initial walking time to the first stop,
- t_{a} time spent waiting for transport,
- t_{p} driving time in all participating vehicles.

As time is commensurate to distance at a given velocity, it is generally assumed that walking speed ranges from 3 to 5 km per hour.

2.2 Interpolation methods

Interpolation is a procedure that estimates a value that lies between two known values. In GIS, interpolation is based on the principle of spatial dependence between near and distinct objects. There are two categories of interpolation techniques: deterministic and statistical, which differ in interpolative functions, the number of input points used in the computation of output values, as well as the area from which the input points are taken (Bielecka, 2006). The most frequently employed deterministic interpolation methods are: *IDW-inverse distance weighted*), *NN- nearest* neighbour, spline and the stochastic method - kriging. The IDW, NN and spline methods enable all measurement points to be included in the calculation (global option) or only the nearest adjacent points (local option). NN interpolation identifies the closest subset of input points to a query point and applies weights to them based on proportionate areas in order to interpolate a value (Sibson, 1981). The surface passes through the input samples, is smooth everywhere except at the locations of the input samples, and works equally well with regularly and irregularly distributed data. *IDW* interpolation determines point values using a linearly weighted (function of inverse distance) combination of a set of input points. It relies on the inverse of the distance raised to the power. When distances are large, or the power value is large, the results may be

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incorrect. Spline is a sufficiently smooth polynomial function that is piecewise defined, it passes exactly through the input points (Childs, 2004).

Kriging assigns weights, referred to as *kriging* coefficients, to the measurement points inside the estimation area in such a way as to minimise kriging variation. Similar to the IDW method, greater weight is assigned to points that lie closer to the input point, but in contrast to IDW, the determined weights are not the basis for distance inversion, but a semivariogram. Kriging is recognised as the best method for the interpolation of unevenly placed phenomena (Childs, 2004; Davis, 1986), but with an isotropic distribution. Therefore, its application for modelling location accessibility by modes of public transport seems unjustified, because the data distribution is isotropic.

2.3 Method of evaluation

The spatial interpolation methods, as any other statistical modelling techniques, produce a certain degree of errors associated with the estimation. Error measurements that have been proposed for evaluation and comparison of interpolation methods are included in several research works, e.g.: Burrough and McDonnell (1998), Isaaks and Srivastava (1989), Li and Heap (2008), Nalder and Wein (1998), and Willmott (1981). Commonly used error measurements include: mean error (ME), mean absolute error (MAE), mean absolute percentage error (MAPE), mean square error (MSE) and root mean square error (RMSE). RMSE and MAE are argued to be among the best overall measures of model performance as they summarise the mean difference in the units of observed and estimated values (Willmott, 1982; Li and Heap, 2008). The mean absolute percentage error (MAPE) is also often useful for purposes of reporting, because it is expressed in generic percentage terms (Li and Heap, 2008).

All mentioned above errors should be calculated on the basis of verification (check) points, distributed randomly over the study area, the number of verification points depends on character of data (ISO 19114, 2003; ISO/DIS 19157, 2011).

Additionally, the number and size of isochronic islands should be analysed. According to literature (Eckert, 1925; Pietrusiewicz, 1996; Rewienska, 1929) the small isochronic islands negatively affect obtained results.

3 CASE STUDY – ACCESSIBILITY OF THE MILITARY UNIVERSITY OF TECHNOLOGY

3.1 Preliminary assumptions and input data

The study, carried out for the Military University of Technology (MUT), gives an analysis of different interpolation methods for drawing up a time-contour map showing estimated travel time to the MUT campus from the whole Warsaw area. It is a "monocentric" map, and the isochrones are "actual" and "centripetal" in character. The measurement points, from which travel times are calculated, were public transport stops located at significant road junctions, by metro and railway stations and also within residential housing estates. The combined travel

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time to the campus was determined for 378 measurement points, as well as for 30 verification (control) points used for assessing accuracy (Figure 1).



Figure 1: Location of measurement and verification points

Public transport timetables for the following services were considered when calculating travel times: buses and trams; suburban rail services (Masovian Railways, Rapid Urban Rail and Warsaw Commuter Rail); and the metro. Data was collected over November and December 2009 and verified in May 2012, noting the travel time during ordinary weekdays at 8.00 am. For each measurement point (stop), the type of transport that would enable the fastest journey to the destination was chosen. The calculations took into account both direct and indirect connections so as to determine the shortest possible journey time. For connections that involved changes, the average waiting time was taken to be 5 minutes. In the case of long distances from stops or stations, where it was necessary to walk to the transport point, it was assumed that pedestrians walk at a speed of 3 km/hour. The total travel time was calculated according to the formula (1). The number of measurement points in travel distance (in minutes) is shown on the histogram (Figure 2). Analysis of the histogram indicates that the least stops are found within isochrones up to 10 minutes and over 100 minutes. The most stops are in areas that are 60 and 90 minutes 'distant' from MUT. This spatial distribution is connected to the spatial management of Warsaw and the location of the Military University of Technology in an outlying district surrounded by woodland.

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Figure 2: The measurement points (stops) in travel time distance (expressed in minutes) to MUT

3.2 Research results

Estimation of accessibility time to the MUT campus was performed with IDW (Figure 3), NN (Figure 4) and *spline* (Figure 5) methods, using the program ArcGIS 9.2. With IDW interpolation a weight coefficient k equals 2; and the area radius - 2000 m. With NN interpolation the coefficient k equals 1.



Figure 3: Time accessibility map for MUT applying IDW

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Figure 4. Time accessibility map for MUT applying NN



Figure 5: Time accessibility map for MUT applying spline - tension

Geodetski vestnik 57/2 (2013) titiet seede Ann boer -tetastitt Avutss or Artsoon MON wencos Anna mut Anns - The Cose of HUNSAW With *spline* interpolation (Figure 5), the initial assumptions concerning minimal spatial curvature and its transition through measurement points can be achieved in two modes - regular and tension. In the regular mode the three derivative functions are minimised, while in tension mode - the first derivative. Experimental calculations were carried out with both methods, utilizing 15 points each time. Results for the tension mode were only marginally better.

4 ANALYSIS AND ASSESSMENT OF RESULTS

Analysis of the isochronic maps for time accessibility of MUT indicate that the fastest journeys to the MUT campus are from the city centre [Centrum] and from places located along the metro. The Ursus district, despite its proximity to the campus, has inconvenient transport connections; consequently travel times can take as long as 45 minutes. On the maps, several isochronic islands were noted. Their number and size are determined by the Warsaw public transport system and the chosen interpolation method. Such islands are located, among others, in the vicinity of railway stations; hence the travel time varies between 45 and 60 minutes, for a distance amounting to approximately 18 km.

Factors most favourable to rapid access are metro and tram line proximity. For places situated at the same distance from the campus, access from those located near the metro is faster by 15-20 minutes (e.g. for places 15 km away from MUT, the journey from Wawer takes 75 minutes whereas from Ursynow only 55 minutes are needed).

In order to assess the quality of each interpolation method, it was necessary to consider estimation errors as well as the number and size of isochronic islands. Absolute error (AE) and absolute percentage error (APE) as well as mean absolute error (MAE), mean absolute percentage error (MAPE), and root mean square error (RMSE) were calculated for 30 verification points, located at different travel time distances from MUT (Figure 1 and Figure 6).



Figure 6: Verification points in travel time function to MUT



Figure 7: Absolute error value (AE) for verification points

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Geodetski vestnik 57/2 (2013) Etsiea Beeeda Ama Bober - RELABULTY ANUSSE OF WIRDE The lowest values and the lowest AE variations in travel time to MUT occurred with *IDW* interpolation, whereas the greatest and most varied occurred with the *NN* method (Figure 7). Furthermore, with *NN* interpolation, the maximum value of AE appears in points lying closest to the boundary of the research area (the boundaries of Warsaw). Using *spline*, where the interpolation surface closely maps the values of measurement points, local anomalies are particularly visible in the form of isochronic islands (Figure 5) and relatively large errors in areas of lowest measurement point density (Figure 1, Figure 7).



Figure 8: Absolute percentage error (APE) value for verification points

It should, however, be noted, that both the AE and the APE for each of the methods are not large. The maximal value of AE amounts to 4.8 minutes, whereas APE amounts to 10%. The mean absolute error (MAE) for each of the methods does not exceed 1.5 minute, the corresponding result for NN equals 1.1 min, for IDW 0.1 min, whereas for spline 0.6 min. The mean absolute percentage error (MAPE) equals 2% for NN, 0.1% for IDW and 1.7% for spline. The smallest RMSE (0. 04 min.) is seen also for IDW method. The values of errors and some statistical parameters of analysed interpolation methods are presented in the Table 1.

	NN	IDW	SPLINE
Mean value	1.88	0.16	0.52
RMSE	0.34	0.04	0.10
MAE	1.11	0.10	0.55
MAPE	1.88	0.16	1.71
Median	1.41	0	0,4
Standard deviation	1.84	0.20	0.55
Variance	3.40	0.04	0.30

Table 1: Comparison of interpolation methods

Significantly greater discrepancy exists between the actual travel time by public transport and the time given in timetables. During the morning peak hours, for places located within the 30 and 45 minute isochrone, the actual journey time (by bus and train) was nearly 20% longer (Table 2).

Number of changes	Actual time	Time from timetable
1	56	46
1	59	49
0	28	23
0	24	20

Table 2: Actual travel time in minutes to MUT, in morning peak hours

Interpolation results differ significantly as regards the number and size of isochronic islands (Table 3). In this analysis, *spline* proved to be the least advantageous. The 16 ha size of an isochrone island means that a single stop with 200 m surroundings is left isolated.

	IDW	NN	SPLINE
Number of isochronic islands of which	15	10	21
<4	1	0	4
4-9	1	0	0
9-16	13	10	17
Min area	1.3	14.6	1.3

Table 3: Number and area [in ha] of isochronic islands

5 CONCLUSIONS

The reliability analysis of interpolation methods applied in travel time map shows that the smallest errors (absolute error, absolute percentage error, RMSE) were seen with *IDW* interpolation, the largest with NN. This is because it is possible to adjust the interpolation parameters for IDW to the specific nature of any given measurement. For both methods, the best results were obtained when the input data was dense and relatively evenly distributed, which is difficult to achieve in lightly built-up areas. The errors clearly decrease when the density of stops increases.

For both *IDW* and *spline* methods, the appropriate choice of input points is very important otherwise inaccessible areas are created.

Mean absolute percentage error (MAPE) is lowest for *IDW*, and highest for *NN*. Taking into account that virtually the whole Warsaw area, beyond the immediate vicinity of MUT, is located within an isochrone of a value greater than 15 minutes, the interpolation errors are small and do not favour the final choice of one of the analysed interpolation methods. Significantly greater are the differences concerning the number and size of isochronic islands. A relatively large number of small isochronic islands occurred when using the *spline* interpolation, which makes it significantly less useful for modelling accessibility time.

The accuracy assessment showed the expected underestimation in travel times. The nature of Warsaw's public transport infrastructure and the high variation of traffic levels during peak hours caused the difference between theoretical and actual MUT accessibility times to vary within a range of 20%.

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