Influence of cooling mode in relation to casting and extrusion parameters on mechanical properties of AA6082

Vpliv načina ohlajanja v povezavi s parametri ulivanja in iztiskanja na mehanske lastnosti zlitine AA6082

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Abstract

In this study, conditional average estimator neural networks (CAE NNs) were used for an analysis of the common influences of the cooling mode in relation to the ram speed, extrusion ratio, casting speed and casting temperature on the yield strength and the elongation of an extruded profile made from aluminium alloy (AA)6082. The obtained results from the analysis revealed very complex relationships between these parameters. In order to maximise the values for the yield strength and the elongation, the values for the ram speed, extrusion ratio, casting speed and casting temperature should be optimised in relation to the mode of cooling.

Key words: AA6082, intermetallic phases, hot extrusion, mechanical properties, neural networks

Izvleček

V tem delu smo uporabili CAE (ang. conditional average estimator, slo. cenilka pogojnega povprečja) nevronske mreže za analizo skupnega vpliva načina ohlajanja v povezavi s hitrostjo bata, iztiskalnim razmerjem, hitrostjo ulivanja in temperaturo ulivanja na mejo tečenja in raztezek iztiskanega profila iz aluminijeve zlitine 6082. Dobljeni rezultati iz analize so pokazali kompleksen vpliv parametrov na mejo tečenja in raztezek. Da lahko izboljšamo vrednosti meje tečenja in raztezka, moramo vrednosti za hitrost bata, iztiskalnega razmerja, hitrosti ulivanja in temperature ulivanja optimizirati v povezavi z načinom ohlajanja.

Ključne besede: AA6082, intermetalne faze, vroče izstiskavanje, mehanske lastnosti, nevronske mreže

Introduction

The use of aluminium alloys (AAs) in the construction and transportation industries has increased in the past decade because of the increasing demand for lightweight constructions and fuel-efficient vehicles [1, 2]. AAs have lower density and medium strength, but compared with construction steels, they have a higher ratio of yield strength to density. So any increase in the mechanical strength would be beneficial to the AA.

There are various steps in the manufacture of AA6082, i.e. melting, casting, homogenisation, extrusion and ageing. In every step of the manufacturing process, the chemical composition and the process parameters have a very complex influence on the final mechanical properties [3-10]. One of these steps is the homogenisation process, which is a crucial heat treatment before the extrusion process for AA production [11, 12]. After casting, the microstructure is not suitable for extrusion and has an inhomogeneous chemical composition, α -Al dendrites with various phases at the borders or in the interdendritic areas. These are usually β -Al₅FeSi, α -Al(FeMn)Si, Al₉Mn₃Si and Mg₂Si, either as single constituents or as complex eutectic clusters [13, 14]. During the homogenisation process, phases such as Mg₂Si dissolve, or transform and change their shape, e.g. needles of β -Al_eFeSi change into spheres of α -Al(FeMn) Si phase. The important part after homogenisation is cooling; a slow cooling speed could lead to the precipitation of Mg₂Si. The second-phase particles in the Al matrix of AA could influence the deformation process [15].

A lot of parameters have a complex influence on the final mechanical properties. But, for large numbers of parameters, the standard experimental methods are not suitable for research of their complex influences on the mechanical properties and are time consuming. For an analysis of the complex influence of the process parameters on the mechanical properties, data collected during the production of AA6082 can be used. The most suitable method for this kind of analysis is that of artificial intelligence, e.g. neural networks. The use of neural networks in metallurgy is relatively new, but some pioneers are already using them [16–20]. In this

study, conditional average estimator neural networks (CAE NNs) were used for an analysis of the cooling mode in relation to the casting and extrusion parameters and their effects on the final mechanical properties.

Experimental

CAE NN analysis

In this study, CAE NN was used to analyse the complex influences of the cooling mode in relation to the process parameters on the yield strength and elongation. The method is especially useful for analysing the unknown influences between various input and output parameters [21]. The observed sample is described by N variables, in our case, the process parameters and the mechanical properties. Each sample is mathematically described by the model vector X_n (Equations 1 and 2). For a complete and correct description of a certain problem, a large quantity of samples is needed. Therefore, the whole phenomenon is described by n set of model vectors, which represent a database (Equation 1).

$$\{X_1, \dots, X_n, \dots, X_N\} \tag{1}$$

$$X_n = \{b_{n1}, \dots, b_{nl}, \dots, b_{nD}, c_{n1}, \dots, c_{nk}, \dots, c_{nM}\}$$
 (2)

Each model vector is composed of two partial vectors B_n (Equation 3) and a truncated vector C_n (Equation 4). The concatenation of both B_n and C_n vectors forms a complete model vector (Equation 2).

$$B_n = \{b_{n1}, \dots, b_{nl}, \dots, b_{nD}\}$$
 (3)

$$C_n = \{c_{n1}, \dots, c_{nk}, \dots, c_{nM}\}$$
 (4)

The prediction vector is also formed of two partial vectors; vector *B* (Equation 5) and an unknown complementary vector (Equation 6).

$$B = \{b_1, \dots, b_l, \dots, b_D\}$$
 (5)

$$\hat{C}_n = \{c_1, \dots, c_k, \dots, c_M\} \tag{6}$$

Fe Si Mn Cu Zn \mathbf{Cr} Ti Mg Min. 0.22 0.80 0.4 0.66 0.02 0.02 0.01 0.01 Max. 0.44 1.24 0.59 0.90 0.10 0.13 0.17 0.04 0.31 0.89 0.47 0.75 0.06 0.04 0.04 0.02 Avg.

Table 1: *Minimum, maximum and average values of chemical composition for AA6082, wt%.*

Notes: Min., minimum; Max., maximum; Avg. average.

The method estimates the unknown complementary vector using a probability density function (Equations 7 and 8), which uses the model vector X_N and the truncated vector B. In this research, the yield strength is estimated from the database and the known process parameters. The Gaussian function (Equation 9) was chosen as a weight function, which is centred at each nth model vector, to obtain the influence of the nth model vector at the point of the prediction vector. In Equation 9, w is defined as a weight function (0.15 in our case), and D is defined as the number of input variables.

$$\hat{C}_k = \sum_{n=1}^N A_n \cdot C_{nk} \tag{7}$$

$$A_n = \frac{a_n}{\sum_{i=1}^N a_i} \tag{8}$$

$$a_n = \frac{1}{2(\pi)^{D/2} w^D} \exp\left[-\sum_{l=1}^{D} \frac{(b_l - b_{nl})^2}{2w^2}\right]$$
 (9)

Equation 9 calculates the intermediate result in the computational process and describes the influence of all the samples and how well they are spread over the problem space. The probability density function (\hat{p}) describes the accuracy of the prediction. The higher the number, the more probable the prediction is and vice versa.

$$\hat{p} = \frac{1}{N} \sum_{n=1}^{N} a_n \tag{10}$$

The results are presented on contour diagrams, with the values of the process parameters on the vertical and horizontal axes. There are two

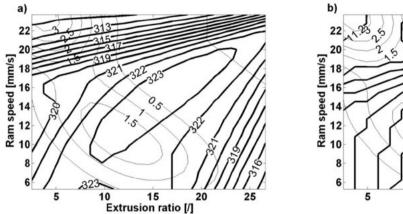
types of values on each contour diagram: the yield strength or elongation, and the probability density function \hat{p} . The reliability of the prediction usually has values in the range from 0.5 to \geq 5. The values for the yield strength and elongation wherein the reliability is <0.5 are generally less accurate.

Database

The data were collected at the Impol Company (Slovenska Bistrica, Slovenia) from different stages of the production process, which involves continuous casting, homogenisation, extrusion and finally ageing. The collected database consists of 3,968 model vectors, which contain data for the process parameters (such as casting speed, casting temperature, extrusion ratio and ram speed), as well as the yield strength and the elongation as the output parameters. Table 1 shows the minimum, maximum and average values for the chemical composition. The process parameters considered in the analysis (Table 2) are the ram speed, extrusion ratio, rate of casting and casting temperature. In Table 2, there are also the minimum, maximum and average values of the yield strength and elongation. After homogenisation, the ingots were cooled in two ways. The first way was cooling by water for 3-4 min (PH). The second way was air-cooling in a chamber with ventilators for 2 h (HH1).

Results and discussion

The results of the analysis are presented in contour diagrams in Figures 1–4. In the following analysis, only those results with prediction reliability higher than 0.5 were considered. The prediction reliability is presented as thin lines in Figures 1–4. On the other hand, the yield strength and the elongation are presented as



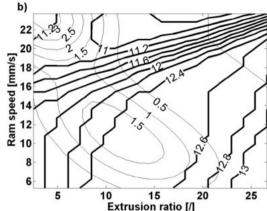


Figure 1: Common influence of ram speed and extrusion ratio on (a) yield strength and (b) elongation with PH cooling mode.

Table 2: Minimum, maximum and average values for extrusion ratio, ram speed, casting speed, casting temperature, yield strength and elongation.

	Extrusion ratio [/]	Ram speed [mm/s]	Rate of casting [mm/s]	Casting temperature [°C]	Yield strenght [MPa]	Elongation [%]
Min.	2.5	5.3	7.2	690	243.23	7.20
Max.	26.6	23.7	7.5	730	365.82	17.39
Avg.	9.1	15.5	7.4	724	319.89	11.97

Notes: Min., minimum; Max., maximum; Avg. average.

thick lines in Figures 1–4. By comparing the different modes of cooling in Figures 1-4, the complex influence of the cooling mode in relation to the values for the ram speed, extrusion ratio, casting speed and casting temperature on the yield strength and elongation can be seen. In Figure 1, the common influence of the ram speed and the extrusion ratio on the yield strength and elongation of the PH cooling mode can be seen. From an extrusion ratio of 5.0 and a ram speed of 22 mm/s, the values for the yield strength (Figure 1a) increase with increasing values for the extrusion ratio and decreasing values for the ram speed. For an extrusion ratio of 15 and a ram speed of 14 mm/s, the values for the yield strength reach maximum values of approximately 323-324 MPa. From this point, the values for the yield strength decrease with increasing values for the ram speed and decreasing values for the extrusion ratio. The values for the elongation (Figure 1b) generally increase from an extrusion ratio of 5 and a ram speed of 22 mm/s, with increasing values for the extrusion ratio and decreasing values for

the ram speed. The maximum values for elongation (12.6–12.8%) in the area of high prediction reliability can be seen for an extrusion ratio of 20 and a ram speed of 7 mm/s.

In Figure 2, the common influence of the ram speed and the extrusion ratio on the yield strength and the elongation of the HH1 cooling mode can be seen. The values for the yield strength (Figure 2a) increase from an extrusion ratio of 3 and a ram speed of 23 mm/s with increasing values for the extrusion ratio and decreasing values for the ram speed, to an extrusion ratio of 17 and a ram speed of 14 mm/s. At this point, the values for the yield strength are a maximum in the range 326-327 MPa. From an extrusion ratio of 17 and a ram speed of 14 mm/s, the values for the yield strength decrease with increasing values for the extrusion ratio and decreasing values for the ram speed, to an extrusion ratio of 25 and a ram speed of 6 mm/s. In this case also, the values for the elongation increase (Figure 2b) with increasing values for the extrusion ratio and decreasing values for the ram speed. But at an extrusion

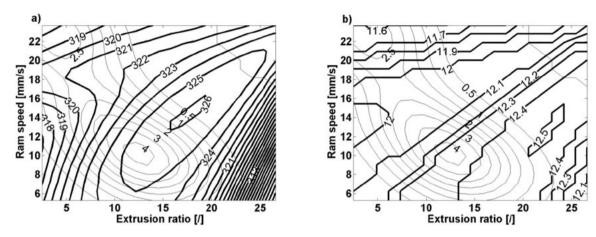


Figure 2: Common influence of ram speed and extrusion ratio on (a) yield strength and (b) elongation with HH1 cooling mode.

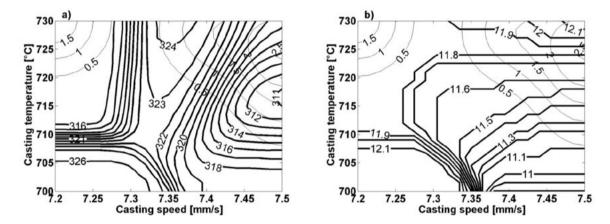


Figure 3: Common influence of casting speed and casting temperature on (a) yield strength and (b) elongation with PH cooling mode

ratio of 22 and a ram speed of 11 mm/s, the values for the elongation reach a maximum value in the range of 12.5–12.6%. From the extrusion ratio of 22 and the ram speed of 11 mm/s, with increasing values for the extrusion ratio and decreasing values for the ram speed, the values for the elongation decrease.

The common influence of the casting speed and casting temperature on the yield strength and elongation in relation to the PH cooling mode can be seen in Figure 3. In the area of the diagram to a casting speed of approximately 7.33 mm/s, the values for the yield strength (Figure 3a) decrease with increasing values for the casting temperature and constant values for the casting speed. In the area of the diagram above a casting speed of 7.35 mm/s, the values for the yield strength decrease with increasing values for the casting speed and constant values for

the casting temperature. At a casting speed of 7.35 mm/s and a casting temperature of 730°C, the values for the yield strength are a maximum and reach approximately 324-325 MPa. As in the case of the yield strength (Figure 3a), in the area of the diagram up to 7.26 mm/s, the values for elongation (Figure 3b) also decrease with increasing values for the casting temperature and constant values for the casting speed. But in the area of the diagram above 7.3 mm/s, the values for the elongation increase with increasing values for the casting temperature and constant values for the casting speed. At the casting speed of 7.5 mm/s and casting temperature of 730°C, the values for the elongation are high and reach approximately 12.1–12.2%.

In Figure 4, the common influence of the casting speed and the casting temperature on the yield strength and elongation in relation to the

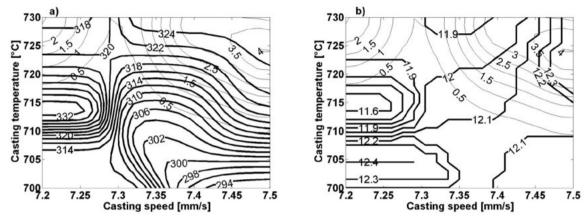


Figure 4: Common influence of casting speed and casting temperature on (a) yield strength and (b) elongation with HH1 cooling mode.

HH1 cooling mode can be seen. In the area of the diagram to the casting speed of approximately 7.29 mm/s, and above casting temperature of 714 °C the values for the yield strength (Figure 4a) decrease with increasing values for the casting temperature and constant values for the casting speed. In the area above a casting speed of 7.3 mm/s, the values for the yield strength increase with increasing values for the casting temperature and constant values for the casting speed. At a casting speed of 7.5 mm/s and a casting temperature of 730°C. the values for the yield strength are a maximum and reach approximately 325-326 MPa. The values for the elongation (Figure 4b) decrease with increasing values for the casting speed and constant values for the casting temperature in the area of the diagram up to a casting speed of 7.3 mm/s and above a casting temperature of 710°C. At a casting temperature of 715°C and a casting speed of 7.23 mm/s, the values for the elongation reach a minimum of 11.6%. In the same area, above a casting temperature of 715°C, the values for the elongation increase with constant values for the casting speed and increasing values for the casting temperature. In the area of the diagram above a casting speed of 7.35 and a casting temperature of 710°C, the values for the elongation increase with increasing values for the casting speed and constant values for the casting temperature. The highest values for the elongation are at a casting speed of 7.5 mm/s and a casting temperature of 720°C, reaching values of approximately 12.3-12.4%.

When comparing the results of the analysis of the common influence of ram speed and extrusion ratio or casting speed and temperature on the yield strength and elongation, the influence of the PH and HH1 cooling modes can be clearly seen. The locations of the maximum values for the yield strength and elongation from Figures 1-2 are gathered in Table 3. In both cases, in Figures 1 and 2, the values for the extrusion ratio and the ram speed of the maximum values for the yield strength and the elongation are not far apart (Figure 1) or nearly coincide (Figure 2). The largest difference can be seen in the analysis in Figure 1. For an extrusion ratio of 15 and a ram speed of 14 mm/s, the values for the yield strength and elongation are high and reach approximately 323-324 MPa and 12.4-12.5%, respectively, which are higher than average (Table 2). The values for the elongation are even higher at an extrusion ratio of 22 and a ram speed of 7 mm/s, reaching approximately 12.6-12.8%, but the values for the yield strength are average (319-320 MPa). When cooling with the HH1 mode, the maximum values for the yield strength and elongation nearly coincide and are high at an extrusion ratio of 22 and a ram speed of 11 mm/s. The values for the yield strength and the elongation reach approximately 326-327 MPa and 12.3-12.4%, respectively, and are higher than average (Table 2). Compared to the PH cooling mode, in which for an extrusion ratio of 15 and a ram speed of 14 mm/s, the values for the yield strength and elongation reach approximately 323-324 MPa and 12.4-12.5% (Table 3), respectively, the

Table 3: Results for maximum values of yield strength or elongation from analysis with corresponding values for ram speed and extrusion ratio for different cooling modes.

Mode of cooling	Max. yield strenght or elongation	Extrusion ratio [/]	Ram speed [mm/s]	Yield strength [MPa]	Elongation [%]
PH	Max. Y.S.	15	14	323-324	12.4-12.5
РП	Max. E.	22	7	319-320	12.6-12.8
HH1	Max. Y.S.	17	14	326-327	12.3-12.4
ппт	Max. E.	22	11	323-324	12.5-12.6

Notes: *E.,* elongation; Min., minimum; Max., maximum; Y.S., yield strength.

Table 4: Results for maximum values of yield strength or elongation from analysis with corresponding values for casting speed and casting temperature of different cooling modes.

Mode of cooling	Max. yield strenght or elongation	Casting speed [mm/s]	Casting temperature [°C]	Yield strength [MPa]	Elongation [%]
PH -	Max. Y.S.	7.35	730	324-325	11.9-12
РП -	Max. E.	7.5	730	316-317	12.1-12.2
HH1 -	Max. Y.S.	7.5	730	325-326	12.3-12.4
ппт	Max. E.	7.5	720	322-324	12.3-12.4

Notes: *E.,* elongation; Min., minimum; Max., maximum; Y.S., yield strength.

values for the yield strength are higher, but the values for the elongation are lower.

In the case of the common influence of casting speed and casting temperature on the vield strength and elongation (Figures 3-4) in relation to the different cooling modes, the maximum values for the yield strength and elongation are concentrated at higher values for the casting speed and the casting temperature. The locations (casting speed and casting temperature) of the maximum values for the vield strength or the elongation from the analysis in Figures 3-4 are gathered in Table 4. In Figure 3, the values for the casting speed and the casting temperature of the maximum values for yield strength or elongation do not coincide. At a casting speed of 7.35 mm/s and a casting temperature of 730°C, yield strength (324-325 MPa) is high, but the values for the elongation are only above average and reach around 11.9-12% (Table 3). On the other hand, at a casting speed of 7.5 mm/s and a casting temperature of 730°C, the values for elongation (12.1–12.2%) are higher, but the values for the yield strength reach approximately 316–317 MPa, which are less than the average values (Table 2). But in Figure 4, with the HH1 cooling mode, high values for the yield strength and elongation coincide at a casting speed of 7.5 mm/s and a casting temperature of 730°C. At this point, the values for the yield strength and elongation reach approximately 325–326 MPa and 12.3–12.4%, respectively, which are higher than the average values (Table 2). In comparison to the PH mode of cooling, where the optimal values for yield strength and elongation reach approximately 323–324 MPa and 11.9–12%, respectively, at a casting speed of 7.4 mm/s and a casting temperature of 730°C, the values for the yield strength and elongation are higher when cooling with the HH1 mode.

Conclusions

From the result of the analysis for the common influence of ram speed and extrusion ratio or casting speed and casting temperature on the yield strength and elongation for different cooling modes, the following conclusions can be drawn:

- The cooling mode in relation to the extrusion ratio and ram speed, or casting speed and casting temperature, has a complex influence on the yield strength and elongation.
- In the analysis of the common influences of ram speed and extrusion ratio, the

PH mode of cooling gives higher optimal values of 12.4–12.6 for the elongation and lower values of 323–324 MPa for the yield strength. The HH1 cooling mode gives higher values for the yield strength (326–327 MPa) but lower values for the elongation (approximately 12.3–12.4%), compared to the PH cooling mode. In both cooling modes, the areas with above-average values for the yield and elongation can be found and are concentrated in the same area, at an extrusion ratio of approximately 15 and a ram speed of approximately 14–17 mm/s.

- The maximum values for the yield strength and elongation are concentrated at higher values of the casting speed and casting temperature, i.e. around 7.35–7.5 mm/s and 720–730°C, respectively.
- When comparing the results of different cooling modes in relation to the common influence of the casting speed and the casting temperature, the HH1 mode of cooling is better than the PH mode of cooling. At a casting speed of 7.5 mm/s and a casting temperature of 730°C, the values for the yield strength and elongation are above average and reach approximately 325–326 MPa and 12.3–12.4%, respectively.
- In order to maximise the values for the yield strength and elongation, the values for the ram speed, extrusion ratio, casting speed and casting temperature should be optimised in relation to the cooling mode.

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