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## On the minimum rainbow subgraph number of a graph

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### Abstract

We consider the Minimum Rainbow Subgraph problem (MRS): Given a graph  $G$ , whose edges are coloured with  $p$  colours, find a subgraph  $F \subseteq G$  of minimum order and with  $p$  edges such that each colour occurs exactly once. This problem is NP-hard and APX-hard. For a given graph  $G$  and an edge colouring  $c$  with  $p$  colours we define the *rainbow subgraph number*  $rs(G, c)$  to be the order of a minimum rainbow subgraph of  $G$  with size  $p$ . In this paper we will show lower and upper bounds for the rainbow subgraph number of a graph.

**Keywords:** Edge colouring, rainbow subgraph.

Math Sci Net: [05C15 \(05C85\)](#)

# O minimalnem mavričnem podgrafovskem številu grafa

## Povzetek

Preučimo problem minimalnega mavričnega podgrafa (MMP): za dani graf  $G$ , čigar povezave so pobarvane s  $p$  barvami, poišči podgraf  $F \subseteq G$  minimalnega reda in s  $p$  povezavami, v katerem da se vsaka barva pojavi natanko enkrat. Ta problem je NP-težak in APX-težak. Za dani graf  $G$  in funkcijo barvanja povezav  $c$  s  $p$  barvami definiramo *mavrično podgrafovsko število*  $rs(G, c)$  kot red minimalnega mavričnega podgrafa grafa  $G$  velikosti  $p$ . V članku podamo spodnje in zgornje meje za mavrično podgrafovsko število danega grafa.

**Ključne besede:** Barvanje povezav, mavrični podgraf.